ANALYSIS

Fishery externalities and biodiversity: Trade-offs between the viability of shrimp trawling and the conservation of Frigatebirds in French Guiana

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Sustainable management of natural resources, and in particular fisheries, must take into account several conflicting objectives. This is the case in the French Guiana shrimp fishery for which profitability objectives imply a reduction in the fishing activity. On the one hand, this fishery has negative externalities on marine biodiversity due to discards. On the other hand, this fishery has positive externalities on the economy of the local community and interestingly enough on a protected seabird species in the area (the Frigatebird that feeds on discards). In this paper, we examine the viability of that system considering two sustainability objectives: an economic objective in terms of the profitability of the fishing activity, and a conservation objective in terms of the Frigatebird population. For that purpose, we have developed a dynamic model of that bioeconomic system and study here the trade-offs between the two conflicting objectives. It provides a means to quantify the necessary give and takes involving the economic and ecological objectives that would ensure a viable management solution. Our study confirms the relevance of the viability approach to address natural resource management issues, which should lead to the development of new tools for the arbitration of conflicting sustainability objectives. In particular, such tools could be used as a quantitative basis for cost–benefit analysis taking into account environmental externalities.

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1. Introduction

Fishery activities generate externalities on biodiversity. On the one hand, there are numerous negative externalities linked to fishery discards in terms of bycatch species and loss of marine biodiversity. Indeed, eliminating discards is currently a major political objective (CEC, 2007). On the other hand, one potential positive externality of these discards is that they may play a fundamental role in marine bird feeding (Furness, 2003). According to Furness (1999), reducing fishery discards may dramatically reduce some seabird populations. This is also the case when discards are reduced due to an adjustment of fishing activities related to the economic context. For example, the prior level of fishing activity of the French Guiana shrimp fishery is no longer economically viable given the present prices, costs, and amount of subsidies. The recent reduction in that fishing activity has resulted in a high rate of Frigatebird chick mortality and has triggered a conflict between the ecological objective of the Frigatebird conservation program off the Caribbean coast of French Guiana and the economic objective of the fishery. Managing fishery activities in a sustainable way must thus take into account conflicting objectives that would ensure economic viability while preserving marine and bird biodiversity.

In ecological economics, it is now recognized that multicriteria modeling, and especially the viability approach (Aubin, 1991), are well-suited to address sustainability issues (De Lara and Doyen, 2008). The aim of the viability approach is to study the consistency between a dynamic model and a set of constraints. It involves defining the conditions such that the constraints are satisfied at all times. In particular, thanks to the viability approach, it is possible to characterize the dynamics of a bio-economic system in terms of its capacity to achieve, in the long-run, sustainability objectives represented by ecological and economic constraints. Béné et al. (2001), Doyen and Béné (2003) and Eisenack et al. (2006) have used the viability approach to investigate natural resource management issues. Cury et al. (2005) have argued that the application of the viability approach is relevant for an ecosystem management of fisheries. Indeed, the viability of fisheries has recently been studied by Doyen et al. (2007), Martinet et al. (2007) and Chapel et al. (2008), among others. In particular, Béné and Doyen (2000) study the viability of the French Guianese shrimp fishery in terms of economic issues alone, without accounting for environmental externalities.

Viability studies usually account for constraints with given levels. It may result in problems with no viable solutions. Martinet and Doyen (2007, appendix A.15) introduced the idea that relaxing some constraints would be one way to overcome from such non-viable solutions. It may also be necessary to conciliate ecological and economic requirements for particular ecological economic states to

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be viable. In this study, we follow this lead to investigate a way to account for potential interactions between constraint levels, using the French Guiana case-study. It is a means to provide much needed information about trade-offs between sustainability objectives. In the example of the shrimp fishery and Frigatebirds, it allows us to describe the trade-offs between ensuring the viability of the shrimp trawling and maintaining the bird population which feeds on fishery discards.

To this end, we have developed a dynamic bioeconomic model of a fishery that generates discards which are a source of food for a bird population. We account for two sustainability objectives (represented by constraints): an economic constraint on the profitability of the fishing activity and a conservation constraint of the bird population. We examine how these sustainability objectives are compatible one with respect to the other, and if there are trade-offs between both viability constraint levels. In other words, we are dealing with how to cope with two seemingly different objectives at the same time, and more specifically with the give and take in the level of constraints that must be worked out to be able to reach these objectives.

The paper is organized as follows. In Section 2, we present a model based on the Guianese shrimp fishery. In Section 3, we address the co-viability issue of achieving at the same time economic and ecological objectives in a dynamic way. In Section 4, we extend this viability analysis by describing the trade-offs between economic and biological objectives. We also define the economic conditions that are necessary (including the minimum amount of subsidies) if the Guianese fishing activity is to be viable while maintaining a targeted Frigatebird population level. In Section 5, we discuss how this approach fits into the literature on biodiversity conservation. In Section 6, we conclude on the potential use of the viability approach as a tool that provides a well-grounded basis for arbitration between conflicting sustainability objectives. Parameter values and mathematical proof are provided in the appendix.

2. Model of a fishery interacting with a seabird population

2.1. The French Guiana case study

The shrimp fishery in French Guiana is composed of trawlers fishing for shrimp on the continental shelf. Two main species are involved: Farfantepeneus subtilis and F. brasiliensis. Only F. subtilis was accounted for. It is the species caught the most often and, since the eighties, it has been thoroughly investigated by Ifremer (the French institute of research for the exploitation of the sea) providing solid knowledge of the population and exploitation dynamics. From a historical point of view, the economic dynamics of the fishery have been characterized by a decrease in the fishing activity for profitability purposes. In turn, the amount of catch has dramatically decreased, and actually it is about half the Maximum Sustainable Yield (MSY). This decrease in fishing activity has meant a decrease in discard.

The Frigatebird Fregata magnificens population in French Guiana is the most important colony of this seabird species from northern Brazil to Venezuela. The colony is located in a natural reserve “Le Grand Connetable”, a small island which makes survey easy. They are exceptional birds, because of their low reproduction rate, their long period of parental care (the longest of any bird), and their long life span (more than 30 years) (Weimerskirch et al., 2003). Before the development of the shrimp fishery (and associated discards), the Frigatebird population was stable, with about 180 nesting couples managing to raise their chick. Since it is not possible here to represent the Frigatebird population accurately, because of their low reproduction rate, their long period of parental care and their long life span (more than 30 years), we assume an opportunistic feeding during nesting period. Based on personal field observation that found 120 Frigatebirds feeding on the discard of a sole shrimp trawler, the same correlation is assumed to hold for the Guianese population. A strong correlation has been also observed between chick mortality during breeding and periods of reduced fishing activity (and associated decreasing discards) within the area of bird foraging (unpublished data). Until recently, the decrease in discard had no impact on the Frigatebird population, but the ongoing decline of the fishery and the associated observed mortality of chicks now jeopardize the conservation program. In the 2007 economic context, some of the 639 surveyed couples were not able to feed their chick. Understanding the interactions between economic dynamics and the conservation objectives is therefore necessary. For that purpose, we have developed a bioeconomic model of the fishery.

2.2. The bioeconomic model

We consider a single stock fishery, characterized every year t by the biomass $B_t$ of the resource stock (shrimp in our case study). The dynamics of the bio-economic system is controlled by the fishing effort $E_t$ following Clark (1985). The global harvest is defined as $H_t = qB_tE_t$, where the constant parameter $q$ represents the catchability of the resource. Using a discrete time version of the “logistic model” to represent the growth function of the shrimp stock, the dynamics of the resource stock is given by

$$B_{t+1} = B_t + R(B_t) - H_t = B_t + rB_t \left(1 - \frac{B_t}{B_{sup}}\right) - qB_tE_t \tag{1}$$

where $B_{sup}$ is the carrying capacity of the ecosystem, and $r$ the natural growth rate of the resource stock ($r < 1$).

The fishery is characterized by profit given as

$$\pi_t = (p + \tau)H_t - cE_t = (p + \tau)qB_tE_t - cE_t \tag{2}$$

where $p$ is an exogenous resource price, $\tau$ is a production subsidy and $c$ is the per effort unit cost.

This fishery generates discards of bycatch species. These discards depend on the fishing effort $E_t$. A part of these discards is used by seabirds to feed themselves and to feed newborns during the breeding season (Frigatebirds in our case study). We define the quantity of discards available for birds as $D_t = dE_t$, where $d$ is a discard constant, i.e., the quantity of discarded biomass that birds can eat per unit of fishing effort. An important point is that the discards are made up of bycatch species (fish, squid, starfish, crabs, jellyfish), hence not proportionally to the catches of the targeted species (to the shrimp biomass) but to the fishing effort (the overall number of trawler’s haul).

We are interested in the number of Frigatebird couples that make a nest and find enough food to raise the chick until it can leave the nest.1 We assume the following relationship between discards and Frigatebird nests

$$F_t = sD_t + F_0 \tag{3}$$

where $F_0$ is the number of Frigatebird couples that raised a chick successfully before fishing began in the area and there was no discard. $s$ is a constant parameter describing the effect of the new food source provided by discards.

2.3. The viability constraints

In the present analysis, we will focus on two viability constraints. On the one hand, the economic viability of the shrimp fishery depends on its profit that has to be positive, i.e., $\pi_t \geq 0$.

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1 Using breeding units as a proxy for the population size is usual when the ecological dynamics is unknown. See, for example, Montgomery et al. (1999).
Defining the catch per unit of effort \( h_t = H_t / E_t \) (for \( E_t > 0 \)), and using the profit definition \((\text{Eq. (2)})\), leads to the following:

\[
\tau_t \geq 0 \rightarrow h_t \geq \frac{c}{p + \tau_t}.
\]

The catch per unit of effort \( h_t = qB_t \) must therefore be greater than a threshold \( h_{\text{min}} = \frac{c}{p + qB_{\text{sup}}} \) for the fishing activity to be profitable. This threshold depends on the economic context (resource price, subsidies level, and cost structure). The viability constraint representing that economic objective is thus defined as

\[
h_t \geq h_{\text{min}}. \tag{4}
\]

On the other hand, an ecological objective is to protect the Frigatebird population. For that purpose, a minimum number of couples able to feed chicks is targeted. The viability constraint representing this ecological objective is thus defined as

\[
F_t \geq F_{\text{min}}. \tag{5}
\]

We aim at defining bioeconomic configurations that make it possible to satisfy both the constraints in a dynamic way.

### 3. Co-viability analysis

#### 3.1. The viability framework of analysis

To develop our analysis, we have adopted the viability approach. The purpose of our analysis is to determine if there are inter-temporal viable exploitation decisions \( E(.) \) that make it possible to satisfy both the economic objective \((\text{Eq. (4)})\) and the conservation objective \((\text{Eq. (5)})\), at all times \( t \geq t_0 \), given the dynamics of the fishery \((\text{Eq. (1)})\).

The approach is based on the definition of states \( B \) and controls \( E \), satisfying dynamics \((\text{1})\) resulting in trajectories that respect constraints \((\text{4})\) and \((\text{5})\). We define the set of states \( B \) from which there exist inter-temporal decisions resulting in viable trajectories. Formally, this set, called the viability kernel of the problem, is defined by

\[
\text{Viab}(h_{\text{min}}, F_{\text{min}}) = \left\{ B_0 \mid \exists E(.) \text{ and } B(.) \text{ starting from } B_0 \text{ satisfying dynamics (1) and constraints (4) and (5)} \forall t \geq t_0 \right\}. \tag{6}
\]

The viability kernel of our problem is determined in subsection 3.2. From any state inside the viability kernel, there exists at least one viable decision driving the dynamic system on a viable trajectory, i.e., a trajectory that respects the constraints at all times. On the contrary, if the state is outside the viability kernel, or if the trajectory leaves it, there are no decisions making it possible to respect the constraints forever, and at least one of the constraints will be violated within a finite time. It means that if state \( B \) is not in the viability kernel, the viability objectives cannot be achieved intertemporally. As a consequence, if the viability kernel is empty, there are no bioeconomic states of the fishery that allows the satisfaction of both economic and ecological constraints in the long run.\(^2\) It means that the sustainability objectives are too ambitious and could never be achieved in the long run, whatever the initial condition of the system. To avoid such an unviable situation, one can relax one of the constraints \((\text{Martinet and Doyen, 2007})\). We will use that approach in Section 4.

#### 3.2. The viability kernel

We provide here the viability kernel of our problem. The proof and mathematical details are in Appendix A.

The expression of the viability kernel depends on the condition

\[
F_{\text{min}} \leq \frac{rsd}{q} \left(1 - \frac{h_{\text{min}}}{qB_{\text{sup}}} \right) + F_0 \tag{7}
\]

An interpretation of this condition is given in the following subsection presenting a sensitivity analysis.

If \((h_{\text{min}}, F_{\text{min}})\) satisfy condition \((7)\), the viability kernel is the set

\[
\text{Viab}(h_{\text{min}}, F_{\text{min}}) = \{B(h_{\text{min}}, B_{\text{sup}})\} \tag{8}
\]

where

\[
B(h_{\text{min}}) = \frac{h_{\text{min}}}{q}. \tag{9}
\]

The associated viable decisions \(E_{\text{viab}}\) must satisfy conditions

\[
E(F_{\text{min}}) \leq E_{\text{viab}} \leq E(B, h_{\text{min}}),
\]

and

\[
E(B, h_{\text{min}}) = \frac{F_{\text{min}} - F_0}{sd} \left(1 + r \left(1 - \frac{B}{B_{\text{sup}}} - \frac{h_{\text{min}}}{q} \frac{1}{B} \right) \right) \tag{11}
\]

If \((h_{\text{min}}, F_{\text{min}})\) do not satisfy condition \((7)\), the viability kernel is empty \((\text{Viab}(h_{\text{min}}, F_{\text{min}}) = \emptyset)\).

When it is not the empty set, the viability kernel is as represented on Fig. 1.

#### 3.3. Sensitivity analysis

When the viability kernel is not empty (i.e., if condition \((7)\) holds), its expression depends on the constraint threshold \(h_{\text{min}}\) (see \text{Eq. (8)}).

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\(^2\) From a mathematical point of view, the viability kernel is a weakly invariant set. It is the biggest set of states such that from any of those states there are admissible decisions resulting in dynamics that both satisfy the viability constraints and remain within the set. This means that from any viable state, at least one dynamic path remains within the viability kernel. Viable decisions are thus defined such that the viability constraints are satisfied and the state of the system stays within the viability kernel.

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**Fig. 1.** Viability kernel (stock biomass) associated with economic constraint \(h_{\text{min}}\) and conservation objective \(F_{\text{min}}\) and associated viable decisions (fishing effort). The straight oblique line represents the stationary state effort-biomass relationship.
Moreover, viable decisions depend on both $h_{\text{min}}$ and $F_{\text{min}}$ (see Eqs. (10) and (11)).

In our viability problem, the economic constraint (4) corresponds to a viability condition depending on the economic context. This context may change (if prices, subsidies, or costs change), resulting in a change in the viability kernel. In a similar way, the ecological constraint (5) is an ecological objective that may be adjusted. We provide here a sensitivity analysis of the results with respect to the levels of the constraints.

From Eq. (9), one can see that $B(h_{\text{min}})$ increases with $h_{\text{min}}$, which means that the higher the economic constraint (the worse the economic context), the higher the induced stock constraint, and then the smaller the viability kernel.

Fig. 2 represents this result. We consider two economic contexts, $h_{\text{min}1}$ and $h_{\text{min}2}$, with $h_{\text{min}2} > h_{\text{min}1}$ meaning that the economic context is more favorable to the fishery in case 1 (higher price and/or subsidy, and/or lower costs); and two ecological objectives $F_{\text{min}1}$ and $F_{\text{min}2}$, with $F_{\text{min}2} > F_{\text{min}1}$, meaning that one wants to maintain a higher Frigatebird population in situation 2.

In Fig. 2, the higher the economic constraint level, the smaller the viability kernel. Moreover, as the threshold $E(F_{\text{min}})$ linearly increases with respect to the constraint level, the viable decisions are reduced when the ecological objective increases.

If the conservation objective is too high, it is not possible to reach the ecological objective for the given economic constraint; the viability kernel is empty (no state makes it possible to satisfy both the constraints over time). From dynamical perspective, if the economic context is degraded (i.e., if $h_{\text{min}}$ increases) the maximum viable effort $E(B)$ decreases, inducing a lower potential conservation of the bird population. There is thus a trade-off between economic viability and ecological conservation. In the next section, we study that point in more detail.

As regards condition (7), we can say that the conservation objective must be lower than a threshold depending on the economic context. The higher $h_{\text{min}}$ is, the lower $F_{\text{min}}$ must be for the viability kernel not to be empty. As we shall see, this condition will play a crucial role in the trade-offs between sustainability objectives.

4. Trade-off between sustainability objectives

In this section, we discuss the consequences of the economic viability of the fishery on the conservation objective of the Frigatebird population. We first provide an analysis describing trade-offs between the economic objective and the biodiversity conservation objective. We then define the economic incentive that would make it possible to reach a given conservation objective, when it is not possible in the initial economic context, and the associated cost.

4.1. Set of reachable objectives

In a given economic context (i.e., for $h_{\text{min}}$ corresponding to given prices, costs and subsidy levels), it would be interesting to know how large a Frigatebird population can be in the long run. To obtain this information, we compute the maximum conservation objective for which the viability kernel is not empty. We define the maximum reachable conservation objective with respect to $h_{\text{min}}$ as follows:

$$\mathcal{F}(h_{\text{min}}) = \max \{ F_{\text{min}} | \text{Viab}(h_{\text{min}}, F_{\text{min}}) \neq \emptyset \}$$  \hspace{1cm} (12)

The non-emptiness of the viability kernel depends on relationship (7). The maximum level $F_{\text{min}}$ that satisfies this condition is

$$\mathcal{F}(h_{\text{min}}) = \frac{\text{rsd}}{q} \left( 1 - \frac{h_{\text{min}}}{qB_{\text{sup}}} \right) + F_0$$  \hspace{1cm} (13)

According to our calculation, given the 2007 economic context, the maximum number of Frigatebird couples expected to successfully breed is (around) $\mathcal{F}(h_{\text{min}}) = 478$ couples, meaning that some of the 639 Frigatebird couples surveyed in 2007 would lose their chick during the nesting period.

We have exhibited a trade-off between the economic constraint $h_{\text{min}}$ and the ecological constraint $F_{\text{min}}$. Achievable conservation objectives must satisfy $F_{\text{min}} \leq \mathcal{F}(h_{\text{min}})$. To increase the level of one of the constraints above the threshold given by compatibility relationship (13), it is necessary to reduce the level of the other.

To provide more information about trade-offs between sustainability objectives, in the following section we examine the give and takes between the conservation objective $F_{\text{min}}$ and the economic objective $h_{\text{min}}$.

4.2. Equivalent economic incentives: One of the costs of biodiversity conservation

In our case study, the economic constraint is defined by the economic context. This constraint can be modified by changing the subsidy level (increasing it or decreasing it). The ecological objective is more flexible as it is a chosen target. It can be adapted in order to have a non-empty viability kernel.

It is possible to define the necessary economic conditions to be able to reach a given conservation objective $F_{\text{min}}$ that is to say to look for the economic conditions resulting in a $h_{\text{min}}$ such that the viability kernel is not empty. For this purpose, we define the reciprocity of relationship (13), i.e., the maximum level of $h_{\text{min}}$ that is compatible with an ecological constraint $F_{\text{min}}$:

$$\mathcal{H}(F_{\text{min}}) = \max \{ h_{\text{min}} | \text{Viab}(h_{\text{min}}, F_{\text{min}}) \neq \emptyset \}$$  \hspace{1cm} (14)

We have

$$\mathcal{H}(F_{\text{min}}) = B_{\text{sup}} \left( 1 - \frac{q(F_{\text{min}} - F_0)}{\text{rsd}} \right)$$  \hspace{1cm} (15)

This level corresponds to the worst economic context compatible with the Frigatebird population objective $F_{\text{min}}$. If the economic situation is worse, i.e., if the economic proxy $h_{\text{min}} = \frac{q}{\beta_0 + \tau_0}$ is higher than the threshold $\mathcal{H}(F_{\text{min}})$, the viability constraints cannot be satisfied. It means that to be able to reach a conservation objective $F_{\text{min}}$, it is necessary to modify the viability constraint $h_{\text{min}}$ (by...
changing the economic context, adjusting the subsidy level) so that the viability kernel is not empty.

As the level of the economic proxy depends on the economic context, one can compute the equivalent shrimp price (including subsidies) at which a given ecological viability objective $F_{\text{min}}$ would be reachable.

$$h_{\text{min}} \leq \mathcal{H}(F_{\text{min}}) \iff \frac{c}{(p + \tau)} \leq q B_{\text{sup}} \left(1 - \frac{q(F_{\text{min}} - F_0)}{r s d}\right)$$

$$\iff (p + \tau) \geq \frac{c}{q B_{\text{sup}} \left(1 - \frac{q(F_{\text{min}} - F_0)}{r s d}\right)}$$

To achieve the conservation objective $F_{\text{min}}$, a minimum fishing activity is needed. That level of fishing activity is profitable only if the selling price (price plus subsidy) is higher than the threshold defined in Eq. (16). As this selling price includes the exogenous market price $p_t$ and the subsidy $\tau$, the minimum level of the subsidy that will result in a non-empty viability kernel is defined as

$$\tau^*(F_{\text{min}}) = \frac{c}{q B_{\text{sup}} \left(1 - \frac{q(F_{\text{min}} - F_0)}{r s d}\right)} - p$$

This level of subsidy can be interpreted as follows: If a conservation objective $F_{\text{min}}$ higher than the value $\mathcal{F}(h_{\text{min}})$ (with $h_{\text{min}} = \frac{c}{(p + \tau)}$) is to be reached, it is necessary to provide an economic incentive at a level $\tau^*$, instead of the initial level $\tau$. In a symmetric way, note that when the viability kernel is not empty (when economic constraint $h_{\text{min}}$ is lower than $\mathcal{H}(F_{\text{min}})$, it is possible to reduce subsidy level from $\tau$ to $\tau^*$ in order to reduce bycatch while still satisfying the conservation objective $F_{\text{min}}$).

By construction, if $\tau = \tau^*(F_{\text{min}})$, then $h_{\text{min}} = \mathcal{H}(F_{\text{min}})$ (the expression of which is given by Eq. (15)). It is possible to compute the minimum cost of such an incentive program by multiplying the subsidy level $\tau^*$ by the minimum quantity of shrimp $H$ harvested in the viability kernel, i.e., at the equilibrium state $\mathcal{E}(h_{\text{min}})$ which is associated to effort $E(F_{\text{min}})$. It reads $H = q B_{\text{sup}} h_{\text{min}} E(F_{\text{min}})$. Moreover $h_{\text{min}} = H/E$, which leads to $H = \mathcal{H}(F_{\text{min}}) E$. As from Eq. (17) $\tau^* = \frac{1}{\mathcal{H}(F_{\text{min}})} - p$, the expression of the minimum total subsidy cost $S(F_{\text{min}})$ can be written as

$$S(F_{\text{min}}) = \left(\frac{c}{\mathcal{H}(F_{\text{min}})} - p\right) \mathcal{H}(F_{\text{min}}) E(F_{\text{min}})$$

$$= \left(c - pq B_{\text{sup}} \left(1 - \frac{q(F_{\text{min}} - F_0)}{r s d}\right)\right) \frac{F_{\text{min}} - F_0}{s d}$$

Eq. (19) only depends on exogenous parameters and on the viability target $F_{\text{min}}$. It is a parabola which is equal to zero when the target $F_{\text{min}}$ is the natural level $F_0$. Fig. 3 represents that cost with respect to the viability constraint $F_{\text{min}}$.

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This level of subsidy can be interpreted as follows: If a conservation objective $F_{\text{min}}$ higher than the value $\mathcal{F}(h_{\text{min}})$ (with $h_{\text{min}} = \frac{c}{(p + \tau)}$) is to be reached, it is necessary to provide an economic incentive at a level $\tau^*$, instead of the initial level $\tau$. In a symmetric way, note that when the viability kernel is not empty (when economic constraint $h_{\text{min}}$ is lower than $\mathcal{H}(F_{\text{min}})$, it is possible to reduce subsidy level from $\tau$ to $\tau^*$ in order to reduce bycatch while still satisfying the conservation objective $F_{\text{min}}$).

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$$S(F_{\text{min}}) = \left(\frac{c}{\mathcal{H}(F_{\text{min}})} - p\right) \mathcal{H}(F_{\text{min}}) E(F_{\text{min}})$$

$$= \left(c - pq B_{\text{sup}} \left(1 - \frac{q(F_{\text{min}} - F_0)}{r s d}\right)\right) \frac{F_{\text{min}} - F_0}{s d}$$

Fig. 3. Total annual cost of a subsidy program $S(F_{\text{min}})$ with respect to the Frigatebirds conservation objective $F_{\text{min}}$. As a benchmark, $\mathcal{F}(h_{\text{min}})$ is the maximum conservation objective that is reachable in the present economic context (without modifying the subsidy level).

5. Discussion

Human activities generate externalities on ecosystems and modify natural equilibria (Crocker and Tschihart, 1992). Worm et al. (2006) emphasize the negative consequences of biodiversity loss in marine ecosystems on the productivity and stability of these ecosystems. The main externality of fisheries on seabird population is negative and due to bycatch (Wilcox and Donlan, 2007). Nevertheless, positive externalities also occur when seabirds feed on discards (Furness, 2003). These externalities should be accounted for in ecosystem approaches to fishery management, considering all the activities that take place in the marine environment and their interdependencies and competition for the ocean space (Pascoe, 2006). To protect biodiversity, seen as a public good, it may be efficient to regulate economic activities to provide good incentives, reducing negative externalities or enhancing positive ones (Bayon et al., 2000). Perhaps the simplest approach to providing correct incentives to private agents is to align private incentives with public economic interest, using Pigouan compensations. This requires setting prices that equate the marginal willingness to pay for biodiversity to the marginal cost of maintaining it (Montgomery et al., 1999). The issue is then to determine at which level biodiversity should be "produced." In particular, the benefits in maintaining or enhancing biodiversity need to be compared with the cost of stopping or maintaining related activities, these costs being direct or indirect. Valuing these different costs and benefits is not easy, especially when one considers non-market goods such as biodiversity. In our case study, the task is all the harder as the objective to maintain a large Frigatebird population conflicts with the objective to reduce bycatch to protect marine biodiversity. According to Eppink and van den Bergh (2007, p.291) "... within particular groups of fragile species and ecosystems, trade-offs in conservation of specific species can be made that may improve the efficiency and effectiveness of conservation efforts, with an eye to the next section, we discuss how this kind of analysis fits into the broader issue of biodiversity conservation.
net effect on biodiversity functions and welfare impact*. This raises the important question of how to deal with conflicting biodiversity preservation objectives.

Metrick and Weitzman (1998) argue that the relevant solution concept to account for biodiversity preservation is the cost–benefit ranking criterion. However, such an approach should rely on “revealed preferences”. Economics provides an important theoretical framework for such valuation and comparison. In economics, the value of a species is often related to its contribution to biodiversity (Brock and Xepapadeas, 2003; Weikard, 2002; Weitzman, 1992, 1998). When based on species preservation, valuation studies focus on a single species, revealing individual willingness to pay to avoid a loss of the given species. This approach may be particularly relevant for endangered or ‘emblematic’ species, to reveal their existence value, even if the result can be biased, but valuing the existence of one particular species is not the same as valuing its contribution to biodiversity. These economic valuation methods provide at least a monetary indicator of preservation value, which can be used in cost–benefit analysis. The main conclusion of Nunes and van den Bergh (2001, p.218) is that “monetary valuation of changes of biodiversity can make sense, if a clear life diversity level is chosen, a concrete biodiversity change scenario is formulated, and a multidisciplinary approach is used.”

The economic modeling approach for biodiversity conservation, including cost-effectiveness models (with a budget constraint), makes it possible to define the “production possibility frontier” of ecological and economic objectives (Eppink and van den Bergh, 2007). Pradhan and Leung (2006) present a way to account for a fishery externality (negative externality of longliners on sea turtles) in a multi-objective fishery management framework. Such an approach makes it possible to assess the success of fishery management within a multi-criteria framework, taking into account the constraints managers face (Ward and Kelly, 2009). According to Wätzold et al. (2006), ecological–economic modeling is a promising way to develop multidisciplinary frameworks. Based on such interdisciplinary ecological–economic approaches, we argue that Viability, which models both economic dynamics and ecological processes, is well-suited to describe the trade-offs between objectives in ecological economic models addressing biodiversity loss and conservation issues, and this from a sustainability perspective, the objectives being met at all times. As suggested by Martinet and Doyen (2007) we extended the viability analysis to describe the necessary trade-offs between conflicting objectives and the quantitative relationships between them. Our results indicate that there is a trade-off between, on the one hand, an increase in fleet profit and thereby a reduction in bycatch and, on the other hand, Frigatebird population size. The preservation of a high population level of Frigatebirds on “Le Grand Connetable” may serve as a source to restore declining populations elsewhere, ensuring their safeguard. The problem is that it implies the reduction in some marine species populations, which has to be taken into account. We are able to quantify this trade-off, giving an expression of the annual cost of Frigatebirds conservation (with respect to the population level) both in terms of required subsidies and discard levels. In particular, we have found that there is an increasing cost of conservation, with decreasing marginal returns to conservation expenditures. This cost of conservation would be enhanced by a monetary valuation of the negative externalities on marine biodiversity and reduced to account for the positive externalities on employment and support to the local community, and compared to the marginal contribution of this Frigatebird population to the species contribution to biodiversity value. By focusing on the relationship connecting local management practice (linked with externalities in the environment of a protected area) to the population of individual species, we do not address the entire chain that connects management decisions to biodiversity. An important issue may be to evaluate the contribution of that Frigatebird population to the safekeeping of the species. In particular, one should take into account ecological threshold effects (Perrings and Pearce, 1994), and the interaction with other (declining) populations, in the strategy of conservation.

According to Metrick and Weitzman (1998, p.21), “Decision about endangered species reflects the values, perception, uncertainties, and contradictions of the societies that make them”. In practice, the expenditures for biodiversity and ecosystem preservation are much lower than the revealed willingness to pay, suggesting that “we do not really care about Biodiversity” (Pearce, 2007). In our case, incentive measures favorable to the Frigatebird population would also have positive social externalities (and micro-economic interests once the fishery gets subsidies). However, negative externalities on marine ecosystem should not be neglected, even if it does not affect emblematic species.

6 This holds true even if valuation of non-market environmental services is better established in terrestrial environment than in marine environment (Pascoe, 2006).

7 The assessment of biodiversity values may lead to a large range of monetary indicators, depending on the biodiversity value type under assessment (e.g., existence value or use value) and the selection of the valuation method, and the interpretation of single species valuation studies should be done with care when the results are used to policy design. Spash and Hanley (1995) emphasize that the monetary willingness to pay revealed by valuation methods (and especially by Contingent Valuation) falls as a measure of welfare change due to the fact that preferences on biodiversity are lexicographic, and it does not allow trade-offs between biodiversity and other market goods. As cost–benefit analysis requires such valuation, it makes it difficult to apply these approaches, and thus to value the benefits of biodiversity preservation (Hanley et al., 1995).

8 This chain includes the links between the population of the species and likelihoods of survival, likelihoods of survival and contributions to biodiversity, and these contributions and the value society places on it (Montgomery et al., 1999).

6 This chain includes the links between the population of the species and likelihoods of survival, likelihoods of survival and contributions to biodiversity, and these contributions and the value society places on it (Montgomery et al., 1999).

9 Note that willingness to pay for squid may be lower than that for Frigatebirds.

6 This holds true even if valuation of non-market environmental services is better established in terrestrial environment than in marine environment (Pascoe, 2006).
an "extra-cost". In this case, it appears that the managers of the conservation program should be aware of this when they define their ecological objective in terms of population number. To sum up, the objectives of a conservation program (within a protected area) cannot be defined without taking into account potential interactions with ecological and economic dynamics outside the protected area.

Our study confirms the relevance of the viability approach to account for ecological and economic objectives in the case of natural resource management issues. Applying this approach makes it possible to define the bioeconomic conditions for several objectives, represented by constraints and given target levels, to be met at all times. We have shown that viability analysis can be extended to account for the give and takes of the constraint levels, making it possible to determine the set of achievable objectives and pinpoint trade-offs between sustainability targets. This extended approach would provide policymakers with thorough knowledge of all the possible achievable objectives, including trade-offs between conflicting ones, and therefore provide a quantitative tool for arbitration. In our study, the description of the trade-offs between sustainability objectives could be a starting point for a broader environmental economic analysis aiming to define the socially optimal level of an incentive program. The cost of fishery subsidies has to be compared to its benefits in terms of social externalities (communities support and employment) and ecological positive externalities (Frigatebird conservation), and its costs in terms of negative externalities on marine biodiversity.

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Appendix A

A.1. Parameter values

We present here the way parameters were obtain, and the hypothesis underlying our model.

A.1.1. Economic and biological parameters for the shrimp fishery

Biological parameters of the shrimp fishery were estimated using LPUE series (landings per unit of effort) as an index of abundance. These LPUE were computed using information from fishing companies log books on fishing time and landings. We used non linear parameter estimation techniques to find the best fit of the predicted LPUE, given the observed LPUE. The fitting criterion is the minimization of the square deviation, using the methods provided by Hilborn and Walters (1992).

Economic parameters (costs, prices, and subsidies) in the 2007 economic context were computed by Huber Fayet. In 2007, the economic context was $p_{2007} = 7$ k-euros per ton; $q_{2007} = 1.1$ k-euros per ton; $c_{2007} = 641.893$ k-euros. These values were defined from economic surveys carried out in May 2007 within the Chaloupe project, in the three major shrimp fishing companies. In the 2007 economic context, the minimum catches per unit of effort ensuring profitability was 79.246 tons of shrimps per effort unit (it corresponds to a resource stock $B = 16,074$ tons). The related viability constraint is $h_{\min} = 79.246$. Note that without subsidies (i.e., if $r = 0$), the fishery would not be profitable at all at the 2007 price and costs.

A.1.2. Frigatebird and fishery interaction parameters

The parameters of the interaction between the Frigatebird population and fishery discards were obtained by Fabian Blanchard and Julien Semelin. We explain here the basic idea underlying relationship (3).

In our model, the fishing effort unit has been defined as the total effort developed by a vessel during one year. Taking into account the maximum individual size of a fish a Frigatebird is capable of swallowing, a trawler haul generates 11.2 kg of discarded biomass the birds can feed on. Computing the mean number of days at sea per vessel and per year (which is quite constant around 258 days at sea per vessel per year in our case study, as climatic conditions in this area are quite similar from one year to another), and accounting for two trawling haul per day, each fishing effort unit $E$ generates $d = 5.78$ tons of discards available as a source of food for birds per year. Given the facts that the bird species has a long life time and a late maturity age, and that data on the population size are available only for recent years, it is not possible to model, according to current knowledge, the population dynamics and the influence of discard on it. We thus have to make some strong assumption on the relationship between discard and reproduction success. The number of nests in natural conditions (the one observed before the development of the fishery in the 60s) is about 180 couples succeeding in reproduction each year. This leads to our reference population $F_{\text{ref}}$. Recent data on discard and Frigatebird population survey, chick mortality occurs every time the quantity of discards decreases below 336 kg per couple. In particular, 215 tons of discards made it possible to ensure the viability of the 639 nests surveyed in January 2007. We assume that discards have a linear effect on reproduction success, and consider two reference points: 180 couples are viable with no discard, 639 couples are viable with 215 tons of discards. It gives us a slope of 2.135 for the linear relationship linking bird couples to discard. Hence the parameters of Eq. (3).

The 2007 survey of Frigatebird population leads to an evaluation of the population size of 639 couples (two adults and a nest). A total conservation objective would results in a threshold $F_{\text{min}} = 639$ (this objective would require to maintain a quantity of discards available for feeding of 215 tons each year).

The following table gives the parameters value for our case study.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Name</th>
<th>Value (Units)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$c$</td>
<td>Resource growth rate</td>
<td>0.91</td>
</tr>
<tr>
<td>$b_{\text{soi}}$</td>
<td>Environmental carrying capacity</td>
<td>18.500 (tons)</td>
</tr>
<tr>
<td>$q$</td>
<td>Resource catchability</td>
<td>4.93 x 10^{-3} (year)^{-1}</td>
</tr>
<tr>
<td>$d$</td>
<td>Rate of “available” discards</td>
<td>5.78 (tons)</td>
</tr>
<tr>
<td>$s$</td>
<td>“Feeding on discards” effect</td>
<td>2.135 (bird couples)</td>
</tr>
<tr>
<td>$F_{\text{soi}}$</td>
<td>“Natural bird population”</td>
<td>180 (bird couples)</td>
</tr>
</tbody>
</table>

A.2. Computation of the viability kernel

We refer to De Lara and Doyen (2008) for the resolution of viability problems in a discrete time framework.

Consider the viability problem defined by the dynamics (1) and the constraints (4) and (5). The aim of the analysis is to define the viability kernel (Eq. (6)) \( \text{Viab}(h_{\text{min}}, B_{\text{min}}, B_{\text{sup}}) \subset B = [0, B_{\text{sup}}] \).

Constraint (4) results in the necessary condition

\[
B_t \geq \frac{h_{\text{min}}}{q} \tag{A.1}
\]

We define the threshold value \( B(h_{\text{min}}) = h_{\text{min}}/q \). The economic constraint (Eq. (4)) is thus equivalent to the state constraint \( B_t \geq B(h_{\text{min}}) \). This constraint is stationary through time.

According to Aubin (1991) and De Lara and Doyen (2008), the viability kernel of the problem is the biggest weakly invariant set within the constrained set \( [B(h_{\text{min}}, B_{\text{sup}})] \), in the sense that:

- from any state \( B_t = \text{Viab} \) there are trajectories staying within \( \text{Viab} \) and respecting the constraints forever (weak invariance of the viability kernel);
- from any state \( B_t = B \) \( \cap \) \( \text{Viab} \) there are no trajectory satisfying the constraint forever.

To prove the results presented in Section 2, we will proceed as follows:

- We introduce some preliminary results
- We then show that the whole constrained domain \([B(h_{\text{min}}, B_{\text{sup}})]\) is viable if condition (7) holds.
- We last prove that the viability kernel is empty if condition (7) does not hold.

**Step 1: Preliminary results**

- Given the ecological constraint (5) and the definition (3), any viable decision must satisfy \( E_t \geq E(h_{\text{min}}) \)

\[
E(h_{\text{min}}) = \frac{F_{\text{min}} - F_0}{sd} \tag{A.2}
\]

- For any \( B_t \geq B(h_{\text{min}}) \), we define the fishing effort \( E(h_{\text{min}}, B_t) \) such that \( B_t + 1 = B(h_{\text{min}}) \). Given the dynamics (1), it reads

\[
E(h_{\text{min}}, B_t) = \frac{1}{q} \left( \frac{1 + r}{1 - \frac{B_t}{B_{\text{sup}}}} - \frac{h_{\text{min}}}{q} \right)
\]

\( E(h_{\text{min}}, B_t) \) satisfies the three following properties:

i) As the dynamics (1) is decreasing with the effort (the higher \( E_t \) the lower \( B_t + 1 \)), for any \( B_t \in [B(h_{\text{min}}, B_{\text{sup}})] \), if \( E_t \leq E(h_{\text{min}}, B_t) \) then \( B_{t+1} \geq B(h_{\text{min}}) \); respectively, we have: if \( E_t \geq E(h_{\text{min}}, B_t) \) then \( B_{t+1} \leq B(h_{\text{min}}) \).

ii) We have

\[
rB(h_{\text{min}}, B(h_{\text{min}})) = \frac{1}{q} \left( 1 - \frac{h_{\text{min}}}{qB_{\text{sup}}} \right)
\]

which is equivalent to

\[
rB(h_{\text{min}}, B(h_{\text{min}})) = qB(h_{\text{min}}) E_t
\]

It means that for \( B_t = B \) and \( E_t = E(h_{\text{min}}, B(h_{\text{min}})) \), the growth of the natural resource is equal to the catches; we have a stationary state, and the resource stock remains at \( B(h_{\text{min}}) \), resulting in an equilibrium.

iii) Note that \( E(h_{\text{min}}, B_t) \) is an inverted U-shape parabola.

On the interval \([B(h_{\text{min}}, B_{\text{sup}})]\), its minimum value is at one of the boundary of the definition set.

Standard computation gives

\[
E(h_{\text{min}}, B(h_{\text{min}})) = \frac{1}{q} \left( 1 - \frac{h_{\text{min}}}{qB_{\text{sup}}} \right)
\]

As \( r < 1 \), we have \( E(h_{\text{min}}, B(h_{\text{min}})) < E(h_{\text{min}}, B_{\text{sup}}) \), which means that

\[
\text{argmin}_{B \in [B(h_{\text{min}}, B_{\text{sup}})]} \ E(h_{\text{min}}, B) = B(h_{\text{min}}).
\]

**Step 2: Proof that the viability kernel is \([B(h_{\text{min}}, B_{\text{sup}})]\) when condition (7) holds.**

We assume that \( F_{\text{min}} \leq \min \left( 1 - \frac{h_{\text{min}}}{qB_{\text{sup}}} \right) + F_0 \) (condition (7)).

From relation (A.1), we know that \( \text{Viab} \subset [B(h_{\text{min}}, B_{\text{sup}})] \). To prove our claimed result, we need to prove that \( B(h_{\text{min}}, B_{\text{sup}}) \subset \text{Viab} \), which leads to the equality of the sets. For that purpose, we only have to show to that there exists (at least) one decision rule that keeps the state of the system within the set \([B(h_{\text{min}}, B_{\text{sup}})]\) while respecting the constraint.

Let us define the following closed-loop decision rule: \( E_t = E(h_{\text{min}}, B_t) \), defined at step 1 above.

From any initial state \( B_t = B(h_{\text{min}}, B_{\text{sup}}) \), we have \( B_{t+1} = B(h_{\text{min}}) \), by definition of \( E(h_{\text{min}}, B_t) \).

Then, according to the properties ii) of \( E(h_{\text{min}}, B(h_{\text{min}})) \) described at step 1, the trajectory is stationary at \( B(h_{\text{min}}) \).

Along this particular trajectory, as \( B_t \geq B(h_{\text{min}}) \) for any \( t \), the economic constraint (4) is satisfied at any time.

Moreover, along that trajectory, for any time \( t \), we have \( E_t \leq E(h_{\text{min}}, B_{\text{sup}}) \).

Using the result iii) exhibited in step 1 that \( E(h_{\text{min}}, B_t) \geq E(h_{\text{min}}, B(h_{\text{min}})) \) for all \( B_t = B(h_{\text{min}}, B_{\text{sup}}) \), we have for all times \( E_t \geq E(h_{\text{min}}, B(h_{\text{min}})) \), where \( E(h_{\text{min}}, B(h_{\text{min}})) = \frac{1}{q} \left( 1 - \frac{h_{\text{min}}}{qB_{\text{sup}}} \right) \) (see step 1, point ii) above).

The condition (7) is equivalent to

\[
\frac{F_{\text{min}} - F_0}{sd} \geq \frac{r}{q} \left( 1 - \frac{h_{\text{min}}}{qB_{\text{sup}}} \right)
\]

We thus get \( E_t \geq E(h_{\text{min}}, B_t) \), which implies that the biological constraint (5) is satisfied, according to the result (A.2) presented at step 1.

For any state within \([B(h_{\text{min}}, B_{\text{sup}})]\), the proposed decision rule leads to a trajectory satisfying the viability constraints at all times.

We thus have \([B(h_{\text{min}}, B_{\text{sup}})] \subset \text{Viab}(h_{\text{min}}, F_{\text{min}}) \).

The viable decisions associated with a given viable states \( B_t \in [B(h_{\text{min}}, B_{\text{sup}})] \) are \( E_{\text{F18/C19}} \) and \( E_{\text{F18/C19}} \) \( \min \) \( E(B) \leq E(\text{F18/C19}) \).

The first inequality is required to the satisfaction of the ecological constraint (see first point of step 1), and the second inequality is required to maintain the state \( B \) within the viability kernel (see step 1, point i)

**Step 3: Proof that the viability kernel is empty when condition (7) does not hold.**

To prove that the viability kernel is empty in that case, we will show that any fishing effort satisfying the ecological constraint (5) would result in a trajectory which would violate the economic constraint (4) in a finite time, whatever the initial condition of the biomass \( B_0 \) such that \( B_0 \in [B(h_{\text{min}}, B_{\text{sup}})] \).

First note that if condition (7) does not hold, we have

\[
F_{\text{min}} \geq \frac{F_0}{sd} \left( 1 - \frac{h_{\text{min}}}{qB_{\text{sup}}} \right) + F_0 \Rightarrow F_{\text{min}} - F_0 \geq \frac{r}{q} \left( 1 - \frac{h_{\text{min}}}{qB_{\text{sup}}} \right).
\]

It means that there exist \( \epsilon > 0 \) such that

\[
F_{\text{min}} - F_0 \geq \frac{r}{q} \left( 1 - \frac{h_{\text{min}}}{qB_{\text{sup}}} \right) + \epsilon \tag{A.3}
\]

Assume for a while that the viability kernel is not empty. It would mean that there is at least one initial state \( B_0 \) such that, from that state, there are admissible decisions resulting in a trajectory that satisfies the constraints forever. We will show that any trajectory satisfying the
ecological constraint (5) would then eventually violate the biomass constraint (A.1), and thus the economic constraint (4). Hence a contradiction.

According to step 1 (A.2), to satisfy the ecological constraint a viable fishing effort must satisfy $E_t \geq \frac{r B_{t+1} - B_t}{B_{sup}}$. Given the biomass dynamics (1), for all $B_t \in [B(h_{min}), B_{sup}]$, we have

$$B_{t+1} - B_t = r B_t \left(1 - \frac{B_t}{B_{sup}}\right) - q B_t E_t$$

$$\iff B_{t+1} - B_t \leq r B_t \left(1 - \frac{B_t}{B_{sup}}\right) - q B_t \frac{r}{q} \left(1 - \frac{h_{min}}{q B_{sup}}\right) + \varepsilon$$

$$\iff B_{t+1} - B_t \leq \frac{B_t}{q} \left(h_{min} - B_t\right) - q B_t \varepsilon$$

On $[B(h_{min}), B_{sup}]$, we obviously have $B_t \geq B(h_{min})$, where $B(h_{min}) = \frac{h_{min}}{q}$. It means that, for any fishing effort satisfying the ecological constraint (5), at each time period, whatever the biomass stock $B_t \in [B(h_{min}), B_{sup}]$, the biomass is necessarily decreasing. Moreover, we also have

$$B_{t+1} - B_t \leq -h_{min} \varepsilon$$

which means that the quantity of resource depleted is larger than the strictly positive level $h_{min}$. There is thus a finite time $T$ such that $B_T = B(h_{min}) + h_{min}$. The biomass constraint (A.1) will then be violated either in $T$ or in $T+1$.

References


